



2D Nonlinear Basement Modeling for Hydrocarbon Exploration by Gravity Data, Carlisle England Area

Yaser Dehban¹, Ali Nejati*¹ and Mohammad Rezaie²

1. Faculty of Mining, Petroleum and Geophysics Engineering, Shahrood University of Technology, Iran

2. Faculty of Engineering, Malayer University, Iran

nejati@shahroodut.ac.ir

DOI: 10.22078/pr.2018.3188.2468

Received: February/18/2018

Accepted: September/02/2018

INTRODUCTION

Gravity in geophysics is an efficient approach to analyze the Earth crust structure, in mineral exploration, Hydrocarbon exploration, hydrogeology, glaciology, etc. The inversion of gravity data to achieve the basement relief of a sedimentary basin has been performed as a common task by the nonlinear techniques [1, 2, 3]. The bottom relief determination of the sedimentary basin is an essential step in Hydrocarbon exploration for prospecting the location of possible stratigraphic traps [4]. It is used in hydrogeology studies to understand the geological structure of aquifers [5, 6], and it is used for reaching the flow rate of discharge in glaciology [7, 8, 9].

METHODOLOGY

In the case of nonlinear inversion data, the following equation (Equation 1) can be written [10]:

$$d=A.m \tag{1}$$

d is the gravity data vector (mGal), A,m are the kernel matrix and model parameter vector (m) respectively.

A nonlinear inverse problems can be solved by minimizing an objective function which depends on the observed and predicted data and defined as follow [11]:

$$F(m)=\frac{1}{2}F_d(m)+\frac{\beta}{2}F_m(m) \tag{2}$$

where β is regularization parameter. If the function F(x) is a smooth function for the model parameters, the function can be limited using the Taylor series for the function which can be written in the following equation (Equation 3) [12]:

$$F(m+\delta m)=F(m)+\gamma^T \delta m+1/2\delta m^T H .m \tag{3}$$

where terms of the gradient vector (γ) and the Hessian matrix (H) can be calculated using the following equations (Equations 4 and 5) [11].

$$\gamma = -(GT(d_0 - d(m)) + \beta I) \quad (4)$$

$$H = G^T G + \beta I - m G^T (d_0 - d(m)) \quad (5)$$

$$G_{ij} = \frac{\partial d_i(m)}{\partial d_j} \quad (6)$$

The derivative G_{ij} can often be found analytically using Equation 6 (8). In equation (5), $\nabla_m G^T$ appears with the data misfit. Moreover, the appearance of $\nabla_m G^T$ with the data describes the nonlinear dependency of the data on the model parameters. Moreover, the nonlinearity is usually weak; therefore, it is neglected in the computation of the Hessian matrix [13].

Finally, the amount of δm can be calculated using subspace method [14]:

$$\delta m = -V(V^T H V)^{-1} V^T \gamma \quad (7)$$

The "T" sign is a transpose matrix and where V is the base vector which is calculated using the singular value decomposition method (SVD) of the matrix Hessian.

RESULT AND DISCUSSION

The obtained results from inversion of synthetic model with free noise and 1% and 5% noise show that the algorithm is stable against data contaminated with different level of noises. Also, data misfit from observed gravity data and predicted data shown that proposed algorithm is good estimate from our model by making a comparison between obtained results from inversion of real gravity data and geological section at the study area.

CONCLUSION

In this method, a set of data for modeling two layers is used and aiding second data is not needed. Also, in this method, basis vectors are used to increase the speed of modeling. Moreover, in this method, the dimension of

inverse matrix is smaller.

REFERENCE

- [1]. Cristina B. V. F., Silva J. B. C. and Medeiros W. E., "Gravity inversion of basement relief using approximate equality constraints on depths," *Geophysics*, Vol. 62, No. 6, pp. 1745-1757, 1997.
- [2]. Blakely R. J. "Potential theory in gravity and magnetic applications," Cambridge University Press, 1996.
- [3]. Vishnubhotla Ch. and Sundararajan N., "3D gravity inversion of basement relief—A depth-dependent density approach," *Geophysics*, Vol. 72., No. 2, pp. 123-132, 2007.
- [4]. Silva, J. B., A. S. Oliveira and Valéria C. B., "Gravity inversion of 2D basement relief using entropic regularization," *Geophysics*, Vol. 75. Vol. 3, pp. 129-135, 2010.
- [5]. Adema G. W., Roy M. B. and Kenneth F. S., "Gravity, Morphology, and Bedrock Depth of the Rathdrum Prairie, Idaho" Idaho Geological Survey, 2007.
- [6]. Bohidar R. N., Jeffrey P. S. and John F. H., "Delineating depth to bedrock beneath shallow unconfined aquifers: a gravity transect across the Palmer river basin," *Groundwater*, Vol. 39. No. 5, pp. 729-736, 2001.
- [7]. Krimmel R. M., "Gravimetric ice thickness determination, South Cascade Glacier, Washington," *Northwest Science*, Vol 44, No 3, pp. 147-153, 1970.
- [8]. Stern T. A., "Gravity survey of the Taylor glacier, Victoria land, Antarctica," Antarctic Research Centre, Victoria University of Wellington, 1978.
- [9]. Venteris E., and Miller M., "Gravitational

profiles on the taku glacier system," Glaciological and Arctic Sciences Institute, University of Idaho, Open File Report, 1993.

[10]. Yaoguo L. and Douglas W. O., "*3-D inversion of gravity data,*" *Geophysics*, Vol. 63, No. 1, pp. 109-119, 1998.

[11]. Lelievre P. G. and Douglas W. O., "*Magnetic forward modelling and inversion for high susceptibility,*" *Geophysical Journal International*, Vol. 166., No. 1, pp. 76-90, 2006.

[12]. Sambridge M. S. "*Non-linear arrival time inversion: constraining velocity anomalies by seeking smooth models in 3-D,*" *Geophysical Journal International*, Vol. 102. No. 3, pp. 653-677, 1990.

[13]. Yanghua W. and Houseman G. A., "*Inversion of reflection seismic amplitude data for interface geometry,*" *Geophysical Journal International*, Vol. 117, No. 1, pp. 92-110, 1994.